## CHEM 361A - Lecture 17 Activity The Approach to Equilibrium

## In Class

1. Consider the interconversion of the 'boat' and 'chair' conformations of cyclohexane

Boat 
$$\underset{k_r}{\overset{k_f}{\underset{k_r}{\longrightarrow}}}$$
 Chair

- (a) If the equilibrium constant, K, at 305 K is  $1 \times 10^2$  and the activation energy,  $E_a$ , for the conversion of the chair conformer to the boat conformer (reverse reaction) is 35 kJ mol<sup>-1</sup> determine the forward and reverse rate constants and the activation energy for the forward reaction at 305 K. Assume that the Arrhenius Equation prefactor, A, is  $1 \times 10^{12}$  s<sup>-1</sup>.
- (b) Find the forward and reverse rate constants at 298 K. Assume that the Arrhenius Equation prefactor, A, is  $1 \times 10^{12} \text{ s}^{-1}$ .
- (c) What is the rate law expression for the rate of change of the concentration of the chair conformation?
- (d) If at t = 0 the [Boat] = [Boat]<sub>0</sub> and [Chair] = 0, show that the integrated rate law expression for [Chair] is

$$[C] = \frac{k_f (1 - e^{-(k_f + k_r)t})[B]_0}{k_f + k_r}$$

- (e) What is  $\tau$  for the return to equilibrium when the temperature is changed from 305 K to 298 K?
- (f) Determine the integrated rate law expression for [Boat]
- (g) Determine the equilibrium concentrations of the Boat and Chair conformations by using their integrated rate law expressions as  $t \to \infty$  at 298 K.
- (h) If the temperature is suddenly increased from 298 K to 1000 K, determine the new equilibrium concentrations and the relaxation constant,  $\tau$ .

## Homework

2. You have an equilibrium process where

$$\mathbf{A} \xleftarrow[\mathbf{k}_r]{\mathbf{k}_r} \mathbf{P}$$

Initially the forward rate constant is equal to  $23.7 \text{ s}^{-1}$  and the reverse rate constant is equal to  $7.8 \text{ s}^{-1}$ . Suddenly, the temperature is changed from 345.2 K to 367.1 K. If the activation energy of the forward process is  $24.1 \text{ kJ mol}^{-1}$ , and the activation energy of the reverse process is  $13.6 \text{ kJ mol}^{-1}$ , determine

- (a) The equilibrium constant, K, at 367.1 K. (K = 3.78)
- (b) The time constant,  $\tau$  for the return to equilibrium. ( $\tau = 0.0202$  s)
- 3. Consider the reaction

$$A + B \xrightarrow[k_r]{k_r} P$$

The temperature was suddenly changed on the system at equilibrium. The time constant was measured to be 310  $\mu$ s, the new equilibrium constant, K, was found to be 0.70, and the new equilibrium concentration of  $[P]_{eq} = 0.20$  M.

- (a) If  $[A]_{eq} = [B]_{eq}$ , determine  $[A]_{eq}$  and  $[B]_{eq}$ . ( $[A]_{eq} = [B]_{eq} = 0.535$ )
- (b) Write an expression of  $\frac{d[P]}{dt}$  using rate laws. Then define [P], [A], and [B] in terms of the new equilibrium and the advancement of the process towards equilibrium, substitute into your rate law expression and integrate in order to show that

$$\tau = [k_r + k_f([A]_{eq} + [B]_{eq})]^{-1}$$

Hint: Prior to integrating, you will have higher order terms of x. You may assume those are small and disregard them.

(c) Determine  $k'_f$  and  $k'_r$  for the new temperature.  $(k'_r = 1844 \text{ s}^{-1} \text{ and } k'_f = 1291 \text{ s}^{-1}).$